# **Unknown Object Manipulation Based on Tactile Information**

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Abstract—This work proposes an approach to manipulate unknown objects based on tactile information. The manipulation can have three goals: the optimization of the hand configuration, the optimization of the grasp quality and the optimization of the object configuration. Three different motion strategies are introduced in order to move the fingers trying to deal with each of the three goals. The strategies can be applied independently or combined in a sequential way. The feasibility of the motion strategies was proven in real experimentation using the Schunk Dexterous Hand SDH2.

#### I. Introduction

Object manipulation using robotic hands equipped with tactile sensors, to detect contacts and increase their capabilities, is a challenging subject in the robotic field. This has impulsed the development of grasping elements with anthropomorphic features, some examples of this elements are the Allegro Hand [1], the Schunk Dexterous Hand [2], the Shadow hand [3], the DLR hand II [4], among others.

Usually, during the object manipulation, it is expected that contact points between the hand and the object are located in specific locations. However, in complex applications the location of the contact points can not be precisely predicted or can not be modeled in advance [5]. In this scenario, tactile information is important for robotic hands since the hands gain in dexterity and precision in object handling when they use tactile feedback. The tactile information obtained during handling can also be used to recognize the shape of unknown objects [6].

The manipulation process usually pursues three goals, one from the hand point of view, one from the grasp (relation hand-object) point of view and one from the object point of view:

- The optimization of the hand configuration: search for a "comfortable" hand configuration while holding the object;
- The optimization of the grasp quality: search for a "secure" grasp such that the hand can resist external force perturbations applied on the object;
- The optimization of the object configuration: search for an "appropriate" object position and orientation to accomplish with the requirements of a given task.

This paper presents an approach to manipulate unknown objects based on tactile information, pursuing these three goals.

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The manipulation of unknown objects has been addressed using different strategies. A method to change the pose of objects of unknown shape using a virtual object frame is introduced in [7], it is based on the triangular fingertip configuration of a three-fingered hand, it also propose a control law to manipulate the object, however the lack of sensorial feedback limits the accuracy of the method. A composite position-force control scheme is presented in [8]. The object relative position with respect to the hand is changed following an input trajectory; the control scheme is evaluated in simulations introducing noise on the sensor measurements to simulate a real environment, however other grasp aspects, as the resulting initial grasp or the stability of the grasp, are not addressed. On the other hand, machine learning techniques have been applied to improve the object manipulation using tactile information, specifically, in order to estimate the grasp stability [9], [10]. Grasp stability can be also achieved using a hybrid force/position controller to perform the grasp of unknown objects by sliding the fingers on the object surface [11]. As a difference with most of the previous works commented above, the proposed approach allows the manipulation pursuing any of the three goals (comfort of the hand, stability of the grasp or object position) as long as their are possible.

The paper is arranged as following. After this introduction, Section II introduces the bases of the addressed problem. Section III discusses the proposed object manipulation approach and the motion strategies to accomplish with the manipulation goals. Experimental results are described in Section IV. Finally, Section V presents the conclusions and future work.

#### II. PROBLEM STATEMENT

This work is focused on the in-hand manipulation problem, in which an unknown object is grasped and manipulated using a robotic hand. The hand has a tactile sensor system, which offers feedback on the contacts between the hand and the object. The object is unknown, i.e. there is not a priori information about the object shape but it is assumed to be rigid. The tactile sensor feedback combined with the kinematic information of the hand is used to manipulate the object avoiding its fall. The presented approach uses tactile feedback to seek the three goals mentioned in the introduction, i.e. optimizing the manipulation action from the point of view of the hand, the object, and the hand-object relationship. The three goals can be pursued independently or as a sequential combination.

Consider a n-dimensional vectorial space defined by the values of the finger joints. Any movement of the fingers is



Fig. 1. Schunk Dexterous Hand (SDH2) with seven *dof* and six tactile sensors arrays, detail of a sensor pad, and graphical representation of the sensor data when the fingertip touches an object showing the contact region and its barycenter.

represented by a curve in this space, whose points indicate the sequence of hand configurations. The manipulation problem can be solved by following an appropriate curve, but finding it is not a trivial problem when the manipulated object is unknown and the manipulation constraints cannot be computed a priori. In this case, planing in advance a precise sequence of movements cannot be done due the lack of information, and therefore it is necessary some exploration method based on on-line sensorial information to find the proper manipulation movements.

The proposed approach deals with the search of the manipulation movements for an unknown object using only the feedback of the tactile information and the hand kinematics, i.e. there is not other information source, like, for instance, visual information. The robotic hand used for the experimentation is the Schunk Dexterous Hand SDH2 [2] shown in Figure 1. This is a three-finger hand with two independent degrees of freedom (*dof*) on each finger, plus another one permitting the rotation of the bases of two fingers allowing them to work opposite to each other in the same plane. The hand has six tactile sensor arrays, one in each phalanx. Each sensor gives information about the relative position of the contact point with respect to the sensor frame, and about the force applied on the object by the corresponding phalanx.

## III. OBJECT MANIPULATION

In this work, the object manipulation is done using two fingertips of the SDH2. The fingers perform a prismatic precision grasp [12], which is comparable with a human grasp using the thumb and index fingers. Thus, the two coupled fingers of the SDH2 are rotated about their bases to work opposite to each other on the same plane. A motion strategy is chosen depending on the goal of the manipulation. The main algorithm and the three motion strategies are introduced in the next subsections.

#### A. Main Algorithm

Algorithm 1 summarizes the procedure used to manipulate an object using tactile feedback. The manipulation starts with an initial blind grasp, where the fingers start their movements from a wide open position and they are closed on the object until a desired force  $F^d$  is reached, then the object is manipulated pursuing the desired goal. Manipulation is an iterative process where each iteration is a manipulation step.

Typical end conditions of the manipulation process are: a stop signal is activated, the manipulation goal is reached, the friction constraints are not satisfied or the fingers reach their workspace limits.

# Algorithm 1: Manipulation with tactile feedback

Input :  $\overline{F^d}$ 

```
1 k = 0
 2 while F_k < F^d do
       Close fingers to grasp the object
       Compute F_k using eq. (1)
 5 while Stop signal is not activated or Goal is not
   reached do
 6
       Compute F_k using eq. (1)
 7
       Compute P_{1_k} and P_{2_k} using Direct Kinematics
       Computed d_{k+1} using eq. (3)
 8
 9
       Compute P_{1_{k+1}} and P_{2_{k+1}} using a Motion Strategy
       if Friction constraints are satisfied and
10
       P_{1_{k+1}} and P_{2_{k+1}} \in workspace of the fingers then
           Move f_1 and f_2 to reach the expected contacts
11
           at P_{1_{k+1}} and P_{2_{k+1}}
           k = k + 1
12
13
       else
           Stop signal activated
14
```

Once the initial grasp is performed, the absolute positions of the initial contact points are computed using the sensor contact information and the hand kinematics, and they are used as initial conditions for the manipulation process. Consider a global reference system located at the base of the finger  $f_1$ , the initial grasp produces two contact points, namely  $P_1$  on finger  $f_1$  and  $P_2$  on finger  $f_2$ . Usually the contact with the object produces a contact region, we consider the barycenter of this region as the contact point and the average force over all the region as the contact force, as proposed in [13] (See Figure 1).

The grasping force  $F_k$  is computed as the average of both contact forces  $F_{1_k}$  and  $F_{2_k}$  measured, respectively, by the sensors of each fingertip,

$$F_k = \frac{F_{1_k} + F_{2_k}}{2} \tag{1}$$

where k denotes the manipulation step.

The distance  $d_k$  between the contact points is given by,

$$d_k = \sqrt{(P_{x1_k} - P_{x2_k})^2 + (P_{z1_k} - P_{z2_k})^2}$$
 (2)

Manipulation is based on a reactive control scheme, in which the current information of the contacts and the kinematic information of the hand are used as inputs. The reactive control action is applied to update  $d_k$  as a function of the measured force, resulting in the controlled distance  $d_{k+1}$  computed as,

$$d_{k+1} = d_k + \Delta d \tag{3}$$

with  $\Delta d$  being a function of the force measured by the tactile sensors according to the follow relationship,

$$\Delta d = \begin{cases} 0 & \text{if } F_{\min} < F_k < F_{\max} \\ +\lambda & \text{if } F_k \le F_{\min} \\ -\lambda & \text{if } F_k \ge F_{\max} \end{cases}$$

where the constant values  $F_{\min}$ ,  $F_{\max}$  and  $\lambda$  must be empirically determined depending on the sensors response. A complete description of the hand kinematics can be found in [14]. The motion strategies and their quality indexes are discussed in the next subsections. A complete review on grasp quality measures can be found in [15].

## B. Motion Strategy 1: Optimizing the hand configuration

When the goal of the manipulation is the optimization of the hand configuration, the joints of the fingers must try to reach the middle-range position avoiding object falls. We consider a quality index  $Q_{\rm PFC}$  that favors the hand configurations with the joints as close as possible to the center of their ranges normalized with corresponding joint ranges [16].  $Q_{\rm PFC}$  is given by,

$$Q_{\text{PFC}} = \sum_{i=1}^{l} \left( \frac{\theta_i - \theta_{0i}}{\theta_{\text{max}_i} - \theta_{\text{min}_i}} \right)^2 \tag{4}$$

where l is the number of joints of the hand,  $\theta_i$  and  $\theta_{0i}$  are the current and the middle-range positions of the i-th joint, respectively, and,  $\theta_{\max_i}$  and  $\theta_{\min_i}$  are the maximum and minimum limits of the i-th joint. The minimization of  $Q_{\rm PFC}$  allows a grasp configuration with a potential wide range of manipulation, since the hand joints are far away from their mechanical limits.

The next configurations of the fingers are easily computed since the middle and the current positions of the joints are known. In this motion strategy, the fingers change their roles in each manipulation step, between leader and follower. The configuration for the leader finger is computed as,

$$\theta_{j_{k+1}} = \theta_{j_k} + (\operatorname{Sign}(\theta_{j_k} - \theta_{0j}) \times \Delta\theta) \tag{5}$$

where the function Sign(x) is given by,

$$\operatorname{Sign}(x) = \begin{cases} -1 & \text{if } x < 0\\ 0 & \text{if } x = 0\\ 1 & \text{if } x > 0 \end{cases}$$

 $\Delta \theta$  is chosen small enough to ensure small changes in the position of the contact point.

The follower finger must adapt its configuration to avoid object falls. We consider the hypothesis that the follower finger moves over a virtual circular path whose radio is given by the distance  $d_{k+1}$  resulting from eq. (3), as shown in Figure 2. Given the coordinates of the leader finger (i.e.  $P_{1_{k+1}}$  for the first iteration), the coordinates of the follower finger  $(P_{2_{k+1}})$  are compute as,

$$P_{z2_{k+1}} = P_{z1_{k+1}} + \left(\tan(\rho)\sqrt{\frac{d_{k+1}^2}{\tan(\rho)^2 + 1}}\right)$$
 (6)

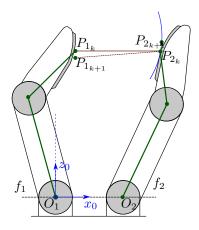


Fig. 2. Two fingers model used for the optimization of the hand configuration.  $\ \ \,$ 

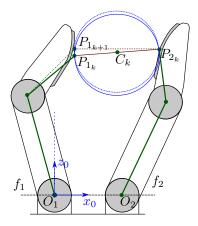


Fig. 3. Two fingers model used for the optimization of the grasp quality.

$$P_{x2_{k+1}} = P_{x1_{k+1}} + \sqrt{d_{k+1}^2 - (P_{z2_{k+1}} - P_{z1_{k+1}})^2}$$
 (7)

where the angle  $\rho$  is computed as,

$$\rho = \arctan\left(\frac{P_{z2_k} - P_{z1_{k+1}}}{P_{x2_k} - P_{x1_{k+1}}}\right) \tag{8}$$

## C. Motion Strategy 2: Optimizing the grasp quality

When the goal of the manipulation is to optimize the grasp quality, the hand have to manipulate the object optimizing the current force closure grasp. We use a quality index  $Q_{\rm DNF}$  that relates the angle between the normal forces at the contact points and the segment between the contact points.  $Q_{\rm DNF}$  favors the finger forces closer to the surface normal. If the segment is close to the boundary of the friction cone, i.e. far from the normal directions, the object could easily slip in presence of perturbations [17].  $Q_{\rm DNF}$  is expressed as,

$$Q_{\text{DNF}} = \frac{1}{n} \sum_{i=1}^{n} |\beta_i| \tag{9}$$

where n is the number of contact points, and  $\beta_i$  is the angle between the normal direction at each contact point and the segment between contact points.

In this motion strategy, we consider the hypothesis that the shape of the object is locally circular, so a proper movement over its shape following the right direction improves the grasp quality. This direction depends on the computed angle  $\beta_i$  for each finger  $f_i$ . The fingers have again different roles (leader and follower) and iteratively change them. The new configuration for the leader finger is computed over the hypothetical circular shape of the object, as a displacement over an arc of circumference  $(d_{k+1}/2) \times \Delta \phi$  as shown in Figure 3, i.e. the circumference arc between  $P_{1_k}$  and  $P_{1_{k+1}}$ .  $\Delta \phi$  can be positive or negative to perform displacements of the contact point in both directions of the fingertip. The sign of  $\Delta \phi$  have to be chosen with the same sign of  $\beta_i$ . This displacement is mapped on the sensor surface changing the contact point on the sensor. The next configuration for the leader finger (i.e.  $P_{1_{k+1}}$ , assuming the leader is  $f_1$ ) is computed as,

$$P_{x1_{k+1}} = C_{x_k} - (d_{k+1}/2)\cos(\Delta\phi) \tag{10}$$

$$P_{z1_{k+1}} = C_{z_k} - (d_{k+1}/2)\sin(\Delta\phi) \tag{11}$$

where the point  $C_k$  is the center of the circumference given by,

$$C_{x_k} = \frac{P_{x2_k} - P_{x1_k}}{2} + P_{x1_k} \tag{12}$$

$$C_{z_k} = \frac{P_{z2_k} - P_{z1_k}}{2} + P_{z1_k} \tag{13}$$

besides, in eq. (10) and eq. (11)  $\Delta \phi$  is chosen small enough to assure small movements of the object on each manipulation step. The next configuration of the follower finger  $(P_{2_{k+1}})$  is computed using the same procedure as in the Motion Strategy 1.

#### D. Motion Strategy 3: Optimizing the object orientation

Another possible goal of the manipulation is the improvement of the object position and orientation looking for a desired one. In this work we consider that the absolute position of the object in the space in controlled by the arm, and therefore only the orientation will be controlled by the fingers, i.e. the finger will care about the object orientation assuming that if this implies a change in the object position the arm will take care of it. Let  $\gamma$  be the object orientation. The orientation resulting from the initial grasp is considered as the reference orientation (i.e.  $\gamma=0$ ). Given a desired orientation  $\gamma_d$  of the object with respect to the one obtained in the initial grasp, the used quality index  $Q_{\rm ROT}$  measures the orientation error (i.e. the angle that the object must be rotated to reach the desired orientation),

$$Q_{\text{ROT}} = |\gamma_d - \gamma_k| \tag{14}$$

where  $\gamma_k$  is the current orientation of the object computed from the hand movements in the iteration k. No other external feedback is considered in the procedure (for instance, the object orientation given by a vision system) although it could exist at a higher level.

In this motion strategy we consider the hypothesis that the fingers are moved over a circular path whose diameter is given by the distance between contact points,  $d_{k+1}$ , as shown in Figure 4. In this case both fingers are moved at same time,

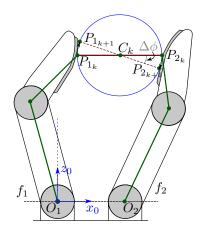


Fig. 4. Two fingers model used for the optimization of the object orientation.

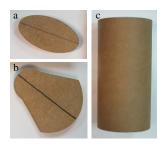


Fig. 5. Three manipulated objects. a) Object 1: elliptical shape; b) Object 2: two-curvature shape; c) Object 3: cylinder.

i.e. they do not have different roles. So, the expected contact points  $P_{\mathbf{1}_{k+1}}$  and  $P_{\mathbf{2}_{k+1}}$  are computed as,

$$P_{x1_{k+1}} = C_{x_k} - (d_{k+1}/2)\cos(\Delta\phi) \tag{15}$$

$$P_{z1_{k+1}} = C_{z_k} - (d_{k+1}/2)\sin(\Delta\phi) \tag{16}$$

$$P_{x2_{k+1}} = C_{x_k} + (d_{k+1}/2)\cos(\Delta\phi) \tag{17}$$

$$P_{z2_{k+1}} = C_{z_k} + (d_{k+1}/2)\sin(\Delta\phi) \tag{18}$$

where  $\Delta \phi$  is chosen positive to turn the object clockwise or negative to turn the object counterclockwise.  $\Delta \phi$  is chosen small enough to assure small movements of the object on each manipulation step. The point  $C_k$  is the center of the circumference, and it is computed using eq. (12) and eq. (13).

## IV. EXPERIMENTAL RESULTS

The described motion strategies have been fully implemented using C++ for the manipulation of unknown rigid objects with the SDH2 hand. Figure 5 shows some rigid objects used in the experimentation. Due to space constraints, only one example is shown for each motion strategy. Each object is held between the two coupled fingers of the SDH2, then the fingers are closed until the detected contact force reach a desired value  $F^d=2\,$  N. Note that the initial contact points are unknown, i.e. the initial grasp configuration changes at each execution of the experiment. After this, the object is manipulated by the two fingers following one of the motion strategies proposed in Section III.

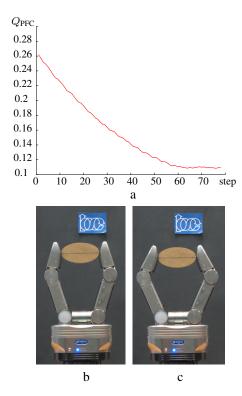


Fig. 6. a)  $Q_{\rm PFC}$  resulting of the manipulation of Object 1; b) Snapshot of the initial grasp; c) Snapshot of the final grasp.

The material of the sensor pads is rubber and the material of the objects is wood or cardboard, thus we consider a worst case friction coefficient  $\mu=0.4$ , which is lower than the friction coefficient between rubber and wood  $\mu=0.7$ , and rubber and cardboard  $\mu=0.5$  [18]. The constant  $\lambda$  to adjust the distance  $d_k$  is set to 1 mm.

### A. Optimizing the hand configuration

The joints of the SDH2 have a range from -90 to 90 degrees, therefore the middle range is 0 degrees, however when the joints are in the middle position the hand is in a singular configuration, thus in this example, each joint range has been adjusted between -90 and 0 degrees for the proximal joints and, between 0 and 90 degrees for the distal joints. The joint variation in each manipulation step was set to  $\Delta\theta=0.5$  degrees. Figure 6a shows the evolution of  $Q_{\rm PFC}$  during the manipulation of Object 1. Note that  $Q_{\rm PFC}$  decreases in each manipulation step, which is an indicator of an improvement in the hand configuration. In this case, the manipulation had a duration of 10,31 s, it ended because  $Q_{\rm PFC}$  did not improve in the last 15 manipulation iterations. Figure 6b and 6c show snapshots of the initial and final grasp configurations.

#### B. Optimizing the grasp configuration

Figure 7a shows the evolution of  $Q_{\rm DNF}$  during the manipulation of Object 2. The parameter to vary the position of the contact points was set to  $\Delta\phi=0.5$  degrees. The manipulation ends when the angles  $\beta_i$  are below a threshold of 0.1 around zero, this happened at 10,74 s. Figure 7b and 7c show snapshots of the initial and final grasp configurations.

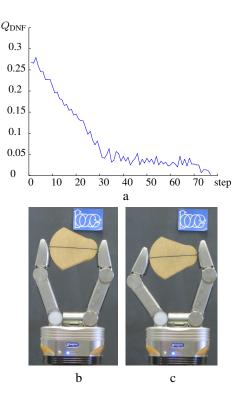


Fig. 7. a)  $Q_{\rm DNF}$  resulting of the manipulation of Object 2; b) Snapshot of the initial grasp; c) Snapshot of the final grasp.

## C. Optimizing the object orientation

In this case, Object 3 was rotated as much as possible in both senses. Figure 8a and 8b show the change in the orientation of Object 3, with respect to the initial grasp, when the object was rotated clockwise and counterclockwise, respectively. The manipulation took 5,32 s in the counterclockwise case and 5,53 s in the clockwise. The manipulation ended when one of the fingers reaches its workspace limits in both executions. Figure 8c shows a snapshot of the initial grasp configuration; Figure 8d and 8e show the final grasp configurations when the object was rotated as much as possible counterclockwise and clockwise, respectively.

# D. Optimizing the hand and grasp configurations

In this example the goal is the improvement of the hand and grasp qualities, using for it a sequential combination of the corresponding individual strategies. First, the object was manipulated until the quality index  $Q_{PFC}$  related to the hand configuration was not improved anymore. Then, the motion strategy to improve the index  $Q_{DNF}$  related to the grasp quality was applied, allowing a variation of  $Q_{PFC}$  within a given threshold (i.e. it can worsen a limited amount). Figure 9 shows the obtained quality indexes  $Q_{PFC}$  and  $Q_{DNF}$  when the Object 3 was manipulated. Even when both quality indexes are shown during the whole manipulation process, until iteration 93 only  $Q_{PFC}$  was considered as an optimization index, using the corresponding motion strategy. At this point, since  $Q_{PFC}$  has not improved for 15 consecutive iterations, the optimization strategy was changed to improve  $Q_{PFC}$ , but now checking that  $Q_{PFC}$  remains within the given threshold.

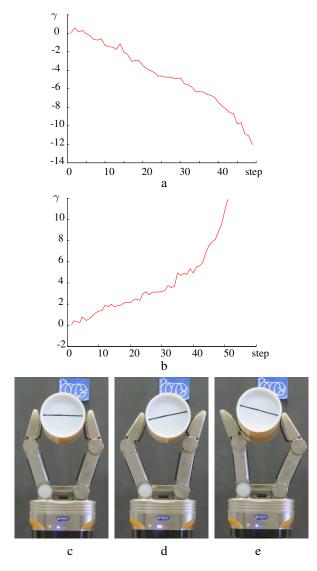


Fig. 8. Orientation resulting of the manipulation of Object 3, when it was rotated a) clockwise; b) counterclockwise. c) Snapshot of the initial grasp. Snapshots of the final grasp when the object is rotated d) counterclockwise; e) clockwise.

The manipulation ended when  $Q_{\rm PFC}$  reached the accepted threshold value, with  $Q_{\rm DNF}$  being less than 0.1, this happened after 28,81 s.

#### V. CONCLUSION AND FUTURE WORK

A manipulation approach based on tactile information and reactive control was presented to manipulate unknown objects. The approach also includes three motion strategies to deal with the optimization of the hand configuration, the optimization of the grasp quality, and the optimization of the object configuration. The experimental results showed that the approach is effective to accomplish with these goals.

An extension of the current implementation is to consider the use of three fingers in the manipulation process, which would allow to consider other quality metrics and also new motion strategies.

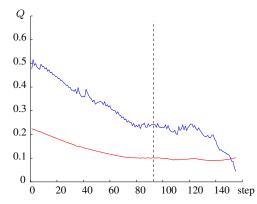


Fig. 9.  $Q_{\rm PFC}$  (in Red) and  $Q_{\rm DNF}$  (in Blue) resulting from apply the strategies to improve  $Q_{\rm PFC}$  until iteration 93, when it has not improved for 10 iterations, then the strategies to improve  $Q_{\rm DNF}$  was applied while  $Q_{\rm PFC}$  remains within a given threshold.

#### REFERENCES

- [1] SimLab Co. Ltd. Allegro Robotic Hand. Site: http://www.simlab.co.kr, Apr 2013.
- [2] SCHUNK GmbH & Co. KG Shunck Dexterous Hand SDH2. Site: http://www.schunk.com, Sep 2011.
- [3] Shadow Robot Co. Shadow Dexterous Hand. Site: http://www.shadowrobot.com, Jan 2010.
- [4] J. Butterfass, M. Fischer, M. Grebenstein, S. Haidacher, and G. Hirzinger. Design and experiences with DLR hand II. In *Proc. World Automation Congress*, volume 15, pages 105–110, 2004.
- [5] M. Meier, M. Schopfer, R. Haschke, and H. Ritter. A probabilistic approach to tactile shape reconstruction. *IEEE Trans. Robotics*, 27(3):630–635, 2011.
- [6] A. Montaño and R. Suárez. Object shape reconstruction based on the object manipulation. In *Proc. IEEE Int. Conf. Advanced Robotics*, pages 1–6. Nov 2013.
- [7] K. Tahara, S. Arimoto, and M. Yoshida. Dynamic object manipulation using a virtual frame by a triple soft-fingered robotic hand. In *Proc. IEEE Int. Conf. Robotics and Automation*, pages 4322–4327, May 2010
- [8] Qiang Li, Robert Haschke, Helge Ritter, and Bram Bolder. Towards manipulation of unknown objects. In *IFAC Symposium on Robot Control*. IFAC, September 2012.
- [9] Yasemin Bekiroglu, R. Detry, and D. Kragic. Learning tactile characterizations of object- and pose-specific grasps. In *Intelligent Robots and Systems (IROS)*, 2011 IEEE/RSJ International Conference on, pages 1554–1560, 2011.
- [10] Hao Dang, Jonathan Weisz, and P.K. Allen. Blind grasping: Stable robotic grasping using tactile feedback and hand kinematics. In Robotics and Automation (ICRA), 2011 IEEE International Conference on, pages 5917–5922, 2011.
- [11] Robert J. Platt. Learning and generalizing control-based grasping and manipulation skills. PhD thesis, UMass Amherst, 2006.
- [12] C.L. MacKenzie and T. Iberall. The Grasping Hand. Advances in Psychology. Elsevier Science, 1994.
- [13] Heinz Worn and Thomas Haase. Force approximation and tactile sensor prediction for reactive grasping. In World Automation Congress, pages 1–6, June 2012.
- [14] A. Montaño and R. Suárez. Getting comfortable hand configurations while manipulating an object. In Proc. IEEE Conf. Emerging Technology and Factory Automation, pages 1–8, Sept 2014.
- [15] Máximo Roa and Raúl Suárez. Grasp quality measures: review and performance. Autonomous Robots, 38(1):65–88, 2015.
- [16] A. Liegeois. Automatic supervisory control of the configuration and behavior of multibody mechanisms. *IEEE Tran. Systems, Man and Cybernetics*, 7(12):868–871, 1977.
- [17] Guanfeng Liu, Jijie Xu, Xin Wang, and Zexiang Li. On quality functions for grasp synthesis, fixture planning, and coordinated manipulation. *Automation Science and Engineering, IEEE Transactions* on, 1(2):146–162, Oct 2004.
- [18] M. Kutz. Mechanical Engineers' Handbook. A Wiley-Interscience publication. Wiley, 1998.